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Marcinkiewicz exponents and jump problem for Beltrami equation

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Abstract

© 2017, Allerton Press, Inc.Marcinkiewicz exponents that were introduced by the author before are applied here to solving boundary-value jump problem on non-rectifiable curve for one special case of the Beltrami equation.

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Keywords

Beltrami equation, boundary-value problem, fractal, Marcinkiewicz exponent, nonrectifiable curve, Riemann problem

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